# Grammar in Performance and Acquisition: interfaces

E Stabler, UCLA

ENS Paris • 2008 • day 2

E Stabler, UCLA Grammar in Performance and Acquisition:interfaces

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- Q1 How are utterances interpreted 'incrementally'?
- Q2 How is that ability acquired, from available evidence?
- Q3 Why are some constituent orders unattested across languages?
- Q4 What kind of grammar makes copying a natural option?
  - we don't need to start from zero (start from grammar)
  - frame explanations supported by convergent evidence

• Everyone<sub>1</sub>, someone saw *t*<sub>1</sub>

'Interpret  $t_1$  as a variable  $x_1$  bound by a higher abstraction.' everyone( $\lambda x_1$ .someone( $\lambda x_2$ .loves $x_1 x_2$ ).

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•  $[t_1 \text{ saw everyone}]_2$ , someone<sub>1</sub> did  $t_2$ 

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GPBC Each trace must be bound throughout the derivation.

(Müller'98 and many others):

- $\begin{bmatrix} VP_2 & t_1 & \text{Gelesen} \end{bmatrix}$  hat  $\begin{bmatrix} \text{das Buch} \end{bmatrix}_1 \begin{bmatrix} \text{keiner } t_2 \end{bmatrix}$ . read has the book noone
- [ $_{VP_2}$ Criticized by his boss  $t_1$ ] John<sub>1</sub> has never been  $t_2$ .
- $[AP_2$  How likely  $[t_1 \text{ to win}]]$  is<sub>3</sub> John<sub>1</sub>  $t_3$   $t_2$ ?
- \*[ $_{AP_2}$ How likely [ $t_1$  to be a riot]] is<sub>3</sub> there<sub>1</sub>  $t_3$   $t_2$ ?
- John  $[_{VP_2}$  reads  $t_1$  [no novels]<sub>1</sub>  $t_2$ .

goals puzzles remnant movement puzzles more basic puzzle

[T]he hypothesis of direct compositionality can be summed up with the following slogan:

#### The syntax and the semantics work together in tandem.

 $\ldots$  it ensures that  $\ldots$  every expression which is computed in the syntax  $\ldots$  actually does have a meaning  $\ldots$ 

To illustrate with a concrete example, consider the standard, non-directly compositional analysis of quantifier scope construal: a verb phrase such as *saw everyone* fails to have a semantic interpretation until it has been embedded within a large enough structure for the quantifier to take scope (e.g. *Someone saw everyone*). On such an analysis, there is no semantic value to assign to the verb phrase *saw everyone* at the point in the derivation in which it is first formed by the syntax (or any other point in the derivation, for that matter). (Barker and Jacobson, 2007, pp.1-2)

(let's worry about this simple case first!)



...the overt structure of "John offended every linguist" ... cannot be the input to the semantic component... The DP "every linguist"... will move out of its VP and adjoin to S in the derivation from SS to LF.

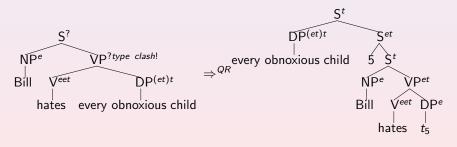


(Heim&Kratzer'86,pp.184-5)

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There is no way to assign a type to the VP-node in our system... The type clash is resolved by May's rule Quantifier Raising (QR)...



(von Stechow'08)

#### Frege: quantifiers as properties of properties of individuals

It is true that at first sight the proposition

"All whales are mammals"

seems to be not about concepts but about animals; but if we ask which animal then we are speaking of, we are unable to point to any one in particular... If it be replied that what we are speaking of is not, indeed, an individual definite object, but nevertheless an indefinite object, I suspect that "indefinite object" is only another term for concept...  $(1884,\, \S47)$ 

 $\dots$  trouble with the semantic paradoxes  $\Rightarrow$  types

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## Syntax

# Church'40 simple type theory (see e.g. Carpenter'97 text)

• Given a set of basic types  $\mathbb{B}$ , we build the whole set of types

 $\mathbb{T} := \mathbb{B} \mid (\mathbb{TT}).$ 

•  $\forall \tau \in \mathbb{T}$ , vars  $V^{\tau}$   $(x_0^{\tau}, x_1^{\tau}, \ldots)$  and constants  $C^{\tau}$   $(c_0^{\tau}, d_1^{\tau}, \ldots)$ 

Terms  $\Lambda := \mathbf{V}^{\tau} \mid \mathbf{C}^{\tau} \mid (\Lambda^{\sigma\tau} \Lambda^{\sigma})^{\tau} \mid (\lambda \mathbf{V}^{\sigma} . \Lambda^{\tau})^{\sigma\tau}$ 

#### • Notation:

across types types associate right abstraction associates right applications associate left application over abstraction

$$\mathbf{V} = \bigcup_{\tau} \mathbf{V}^{\tau} \qquad \mathbf{C} = \bigcup_{\tau} \mathbf{C}^{\tau}$$
  

$$eet = e(et)$$
  

$$\lambda x. \lambda y. \lambda z. M = \lambda x. (\lambda y. (\lambda z. M))$$
  

$$fabc = ((fa)b)c)$$
  

$$\lambda x. fxy = \lambda x. ((fx)y)$$

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## semantics

- For each basic type  $au \in \mathbb{B}$ ,  $\textit{Dom}_{ au}$  is a set
- For all other types  $\mathbf{Dom}_{\alpha\beta} = [\mathbf{Dom}_{\alpha} \rightarrow \mathbf{Dom}_{\beta}]$
- Frame  $\mathbf{Dom} = \bigcup_{\alpha \in \mathbf{Typ}} \mathbf{Dom}_{\alpha}$
- Model *M* = ⟨Dom, [[.]]⟩, where
   Dom is a frame, and
   [[.]] : C → Dom such that if α ∈ C<sub>τ</sub> then [[α]] ∈ Dom<sub>τ</sub>
- Assignments  $\theta: V \to Dom$  such that  $\theta(x) \in \mathbf{Dom}_{\alpha}$  if  $x \in \mathbf{V}^{\alpha}$
- Denotations wrt  ${\cal M}$  and heta,

$$\begin{split} \llbracket x \rrbracket_{\mathcal{M}}^{\theta} &= \theta(x) \text{ if } x \in \mathbf{V}, \\ \llbracket c \rrbracket_{\mathcal{M}}^{\theta} &= \llbracket c \rrbracket \text{ if } c \in \mathbf{C}, \\ \llbracket \alpha \beta \rrbracket_{\mathcal{M}}^{\theta} &= \llbracket \alpha \rrbracket_{\mathcal{M}}^{\theta} \llbracket \beta \rrbracket_{\mathcal{M}}^{\theta}, \\ \llbracket \lambda x. \alpha \rrbracket_{\mathcal{M}}^{\theta} &= f \text{ such that } fa = \llbracket \alpha \rrbracket_{\mathcal{M}}^{\theta[x:=a]}. \end{split}$$

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quantifiers and arguments Simple type theory (Church'40) Extensions Quantifiers

(Syn) Basic types  $\mathbb{B} = \{e, t\}$ , and for each type  $\tau$ , constants

 $\begin{array}{ll} \mathsf{not} \in \mathsf{C}^{tt} & \mathsf{and} \in \mathsf{C}^{ttt} \\ \mathsf{eq}_{\tau} \in \mathsf{C}^{\tau\tau t} & \mathsf{everything}_{\tau} \in \mathsf{C}^{(\tau t)t} \\ \iota_{\tau} \in \mathsf{C}^{(\tau t)\tau} \end{array}$ 

(Sems)  $\mathbf{Dom}_{t} = \{\text{true, false}\}, \mathbf{Dom}_{e} \text{ any set of individuals, and constants are interpreted as follows:$  $<math display="block">[[\mathbf{not}]](x) = \text{true if } x = \text{false, false otherwise}$   $[[\mathbf{and}]](x)(y) = \text{true if } x = \text{true and } y = \text{true, false otherwise}$   $[[\mathbf{eq}_{\tau}]](x)(y) = \text{true if } x = y, \text{ false otherwise}$   $[[\mathbf{everything}_{\tau}]](P) = \begin{cases} \text{true if } \forall \mathbf{a} \in \mathbf{Dom}_{\tau}, P(\mathbf{a}) = \text{true} \\ \text{false otherwise} \end{cases}$   $[[\iota]](P) = a \text{ if } a \text{ is the unique thing such that } P(a) = \text{true.}$ 

Instead of everything<sup>(et)t</sup>, Church has  $\Pi$  and Carpenter has every, with some<sup>(et)t</sup> or something introduced by definition.

quantifiers and arguments

Simple type theory (Church'40) Extensions Quantifiers

# (limited) polymorphism

Easy extensions are available for limited polymorphism.
 E.g. instead of eq<sub>τ</sub> for each type τ, in λ<sub>2</sub>,

$$\mathbf{eq} = \mathbf{\Lambda}\alpha.\lambda \mathbf{x}^{\alpha}.\mathbf{x}^{\alpha}$$

E.g. instead of type shifting (cf Capretta'02),  $\forall n \in \mathbb{N}$ 

 $p_0 = t.$   $p_{n+1} = ep_n.$  everything  $p_{n+1}p_n$ .

(Barendregt'92 survey linked on web page)

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quantifiers and arguments Quantifiers and arguments Quantifiers

(Syn) Add logical constants every, some  $\in C^{(et)(et)t}$ and constants person, thing  $\in C^{et}$ , saw  $\in C^{eet}$ .

$$[[some PQ]] = \begin{cases} true & \text{if } Pa \to Qa, \text{ all } a \in \mathbf{Dom}_e \\ false & \text{otherwise} \end{cases}$$
$$[[some PQ]] = \begin{cases} true & \text{if } Pa = Qa = true, \text{ some } a \in \mathbf{Dom}_e \\ false & \text{otherwise} \end{cases}$$

(E.g.) Then we have formulas like these

(every person)( $\lambda y$ .(some thing)( $\lambda x$ .sawxy))

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for VP=[binary relation+quantifier], two main approaches:

 saturate relation, abstract to bind var, then apply quantifier (Heim&Kratzer, von Stechow,...)

(some person)( $\lambda y$ .(every thing)( $\lambda x$ .sawxy))

2. type-shift (Hendriks, Jacobson, Barker, Winter,...).

 $L = \lambda Q^{(et)t} . \lambda R^{eet} . \lambda y . Q(\lambda x. Rxy)$ (some person)(L(every thing)saw)

2'. simply assume quantifiers are polymorphic (Keenan,...)

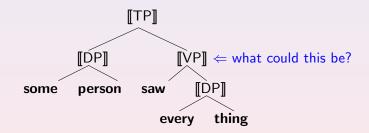
### (some person)((every thing)saw)

(NB: in all 3 approaches, (some person) has the identical argument, provided by VP)

So let's adopt Keenan's simple 'arity reducer' perspective, but use QR to establish scope...

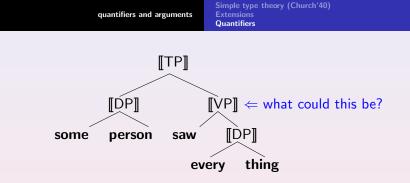
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What could VP denotation be, on a standard QR story?



- Scope determined by 'landing position' of object.
- Roughly, from [VP] we need (every thing) $\lambda x$  and sawx

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• Roughly, from [[VP]] we need (every thing) $\lambda x$  and sawx

Two technical issues: (cf. Kobele'06, PL sems)

- Variable x has to be 'fresh' to avoid accidental capture
- What is λx?

But for MG interpretation, these issues can be avoided.

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#### Basic idea:

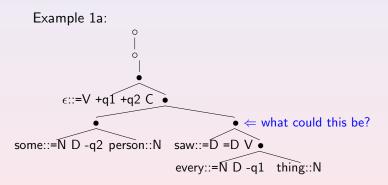
- In MGs, QR triggered by some feature of DP (e.g. -q,-top)
- Call a tree *useful* if it occurs in a completed derivation
- By SMC, no 2 constituents in any useful tree have the same initial licensee feature
- So if some subset of the licensee features  $L = \{-f_1, \ldots, -f_k\}$ , trigger DP movement to interpreted positions, we represent the meaning of each useful tree with a k + 1-tuple:

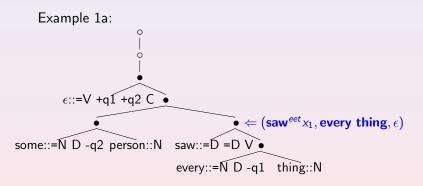
$$(s_0, s_1, \ldots, s_k),$$

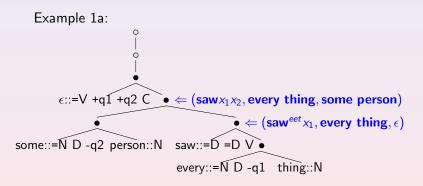
with  $s_0$  the semantic value of the head, and each other  $s_i$  the value of the subtree (if any) moving for feature  $-f_i$ .

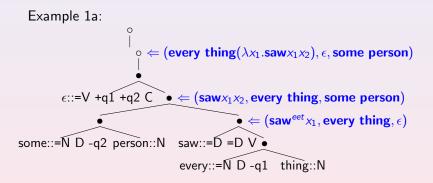
We will consistently use variable x<sub>i</sub> for feature s<sub>i</sub>, so if a constituent moves first for -f<sub>1</sub> and then for -f<sub>2</sub>, after the first movement we equate x<sub>1</sub> = x<sub>2</sub> and immediately bind x<sub>1</sub>.

(similar association of variables with structural positions, with finite bounds, will be available with most modifications of the SMC considered on the first day)

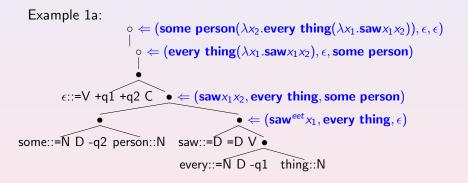




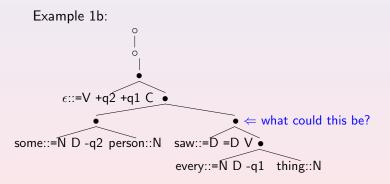


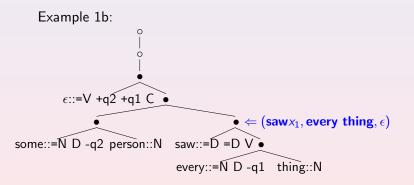


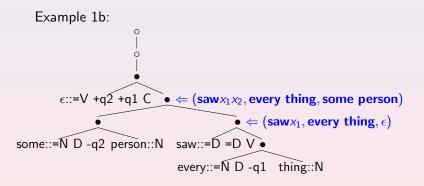
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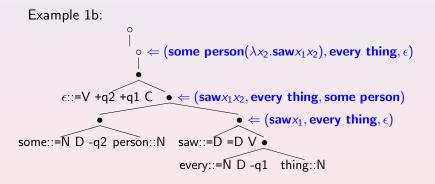


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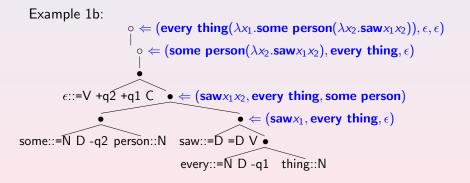








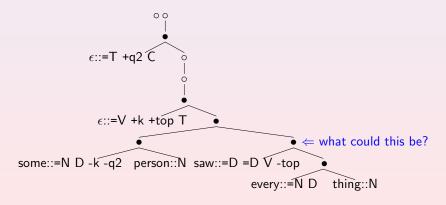
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semantics for MGsSketch<br/>Example: remnant movementHiraiwa'02:Someone saw everyone $(\exists > \forall, \forall > \exists)$ Saw everyone, someone did $(\exists > \forall, *\forall > \exists)$ 

 $*\forall > \exists\;\; \text{if SpIC}$  or other constraint blocks q-movement from spec,TP



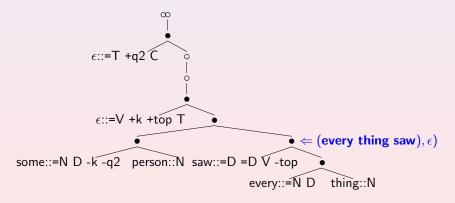
A (10) × (10) × (10) ×

Sketch semantics for MGs Example: remnant movement Hiraiwa'02: Someone saw everyone  $(\exists > \forall, \forall > \exists)$ 

Saw everyone, someone did  $(\exists > \forall, *\forall > \exists)$ 

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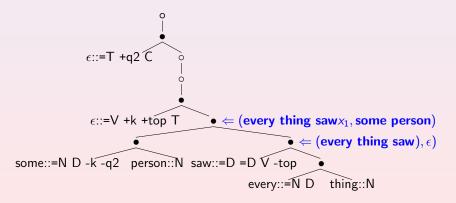
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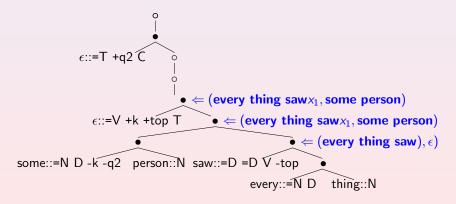
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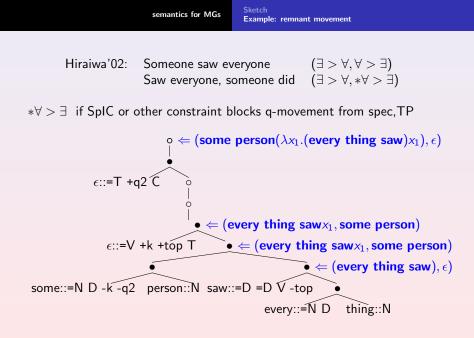
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Appendix: semantics for MGs

Detail summary Example: checking Improvements

- Consider MG with some subset of features  $L = \{-f_1, \ldots, -f_k\}$  (including e.g. -q, -foc), triggering DP movement to clause peripheral positions where they can be interpreted. Everything else interpreted in base position.
- Tree t is useful iff it occurs in a completed derivation
- Interpret useful tree t as a tuple,  $[\![t]\!] = (s_0, s_1, \dots, s_k)$  where
  - $s_0$  is the semantic value of the *t*-head, and for  $1 \le i \le k$ ,
  - $s_i$  is the semantic value of the  $-f_i$  head, if any, otherwise  $\epsilon$
- Given  $(s_0, ..., s_k)^{[i:=x]} = (s_0, ..., s_{i-1}, x, s_{i+1}, ..., s_k)$

(Sometimes we have a sequence of substitutions to make  $[i_1 := x_1, \ldots, i_n := x_n]$ , all  $i_i$  distinct)

- Given  $s = (s_0, s_1, \dots, s_k)$  and  $t = (t_0, t_1, \dots, t_k)$  let  $(s+t) = (u_0, \dots, u_k)$  where  $u_i = s_i$  if  $s_i \neq \epsilon$ , else  $u_i = t_i$ .
- FF(t) = f means the first feature of head of tree t is f

Appendix: semantics for MGs

Detail summary Example: checking Improvements

For 
$$t_1[=c] = a$$
 with  $\llbracket a \rrbracket = (s_0, \ldots, s_k)$ ,  
and  $t_2[c] = b$  with  $\llbracket b \rrbracket = (r_0, \ldots, r_k)$ ,

$$\llbracket \mathbf{em}(a,b) \rrbracket = \begin{cases} (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=s_0x_i,i:=r_0]} & \text{if } FF(t_2) = -f_i \in L \quad (store) \\ (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=s_0r_0]} & \text{if } s_0r_0 \text{ well-typed} \quad (FA) \\ (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=r_0s_0]} & \text{otherwise} \quad (BA) \end{cases}$$

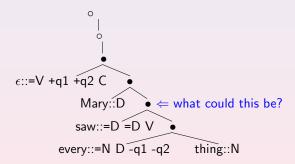
For 
$$t_1[+f_j] = a$$
 with  $\llbracket a \rrbracket = (s_0, \ldots, s_k)$ , with subtree  $t_2[-f_j]$ 

$$\llbracket im(a) \rrbracket = \begin{cases} \llbracket a \rrbracket & \text{if } FF(t_2) = -f_i, i = j \quad (ck) \\ \llbracket a \rrbracket^{[0:=some(\lambda x_j. x_i = x_j \land s_0), i:=s_j, j:=\epsilon]} & \text{if } FF(t_2) = -f_i \in L \quad (ck) \\ \llbracket a \rrbracket & \text{if } FF(t_2) \notin L \quad (0) \\ \llbracket a \rrbracket^{[j:=\epsilon, 0:=s_j(\lambda x_j. s_0)]} & \text{if } t_2 \text{ has no features. } (bnd) \end{cases}$$

(nb: in these defs, sequences of cases are to be understood in order, as if...else, and some is obviously (et)t.)

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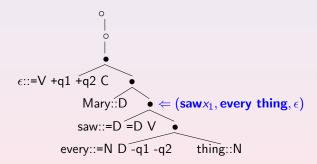
### checking example:



Again, to make the VP easier to point to, I put subject first, but selected subj is the 2nd arg of em)

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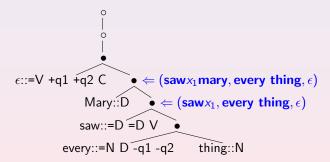
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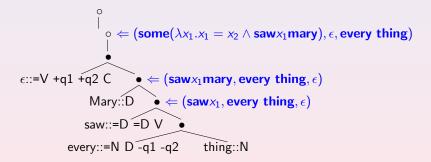
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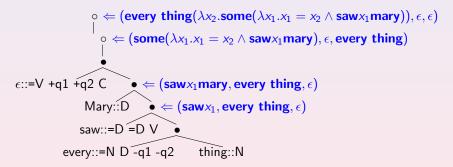
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checking example:



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Appendix: semantics for MGs

Detail summary Example: checking Improvements

# Improvements

• can we make [[move]] uniform?

 when we don't know scope of object, does anything more follow about VP denotation that the pairs do not make explicit?

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Appendix: semantics for MGs

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# Improvements

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yes, and this gets us closer the the representational perspective – but too much for today

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Appendix: semantics for MGs

Detail summary Example: checking Improvements

# Improvements

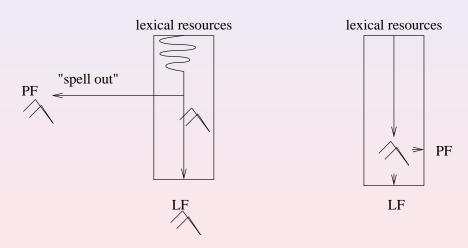
• can we make [[move]] uniform?

yes, and this gets us closer the the representational perspective – but too much for today

## when we don't know scope of object, does anything more follow about VP denotation that the pairs do not make explicit?

yes, remember conservativity! This is important and usually ignored (but cf. Ben-Shalom, Keenan) – too much for today

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the king eat -s the pie

 $\mapsto \quad \text{the king eats the pie} \quad$ 

(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)

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the king eat -s the pie	$\mapsto$	the king eats the pie
the king have -s eat -en the pie	$\mapsto$	the king has eaten the pie

(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)

(ロ) (同) (E) (E) (E)

the king eat -s the pie the king have -s eat -en the pie the king have -s laugh -en

- $\mapsto \quad \text{the king eats the pie} \quad$
- $\mapsto$   $\;$  the king has eaten the pie
- $\mapsto \quad \text{the king has laughed} \quad$

(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)

- the king eat -s the pie the king have -s eat -en the pie the king have -s laugh -en the king be -s laugh -ing
- $\mapsto \quad \text{the king eats the pie} \quad$
- $\mapsto \quad$  the king has eaten the pie
- $\mapsto \quad \text{the king has laughed} \quad$
- $\mapsto \quad \text{the king's laughing} \quad$

(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)

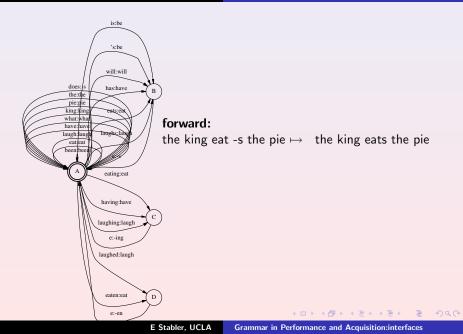
- the king eat -s the pie the king have -s eat -en the pie the king have -s laugh -en the king be -s laugh -ing the king will -s laugh
- $\mapsto$  the king eats the pie
- $\mapsto$   $\;$  the king has eaten the pie
- $\mapsto \quad \text{the king has laughed} \quad$
- $\mapsto$  the king's laughing
- $\mapsto$  the king will laugh

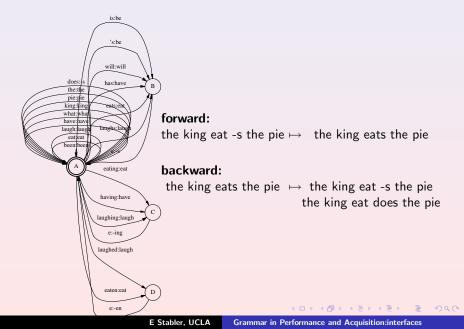
(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)

the king eat -s the pie the king have -s eat -en the pie the king have -s laugh -en the king be -s laugh -ing the king will -s laugh -s the king laugh

- $\mapsto$  the king eats the pie
- $\mapsto$   $\;$  the king has eaten the pie
- $\mapsto \quad \text{the king has laughed} \quad$
- $\mapsto \quad \text{the king's laughing} \quad$
- $\mapsto \quad \text{the king will laugh} \quad$
- $\mapsto \quad \text{does the king laugh}$

(CL: Roark&Sproat'07,Huet'03) (Ph: Riggle'04,Eisner'97)





- simple formalisms can model many linguistic proposals
- a straightforward semantics values every constituent in course of derivation
  - $\bullet$  Simple, extensional MG semantics is defined in  $\approx \! 7$  lines
  - No problem with remnant movement
  - Conditions could be placed on use of LF variables (cf Collins&Sabel)
  - A tighter connection than pairing for VP is possible
- PF standardly handled by transducer composition
- Q1 What performance models allow incremental interpretation (and remnant movement, doubling constructions)?

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intermission 2 References

So far 2

# MG semantics

For 
$$t_1[=c] = a$$
 with  $\llbracket a \rrbracket = (s_0, \dots, s_k)$ ,  
and  $t_2[c] = b$  with  $\llbracket b \rrbracket = (r_0, \dots, r_k)$ ,

$$\llbracket \mathbf{em}(a,b) \rrbracket = \begin{cases} (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=s_0x_i,i:=r_0]} & \text{if } FF(t_2) = -f_i \in L \quad (store) \\ (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=s_0r_0]} & \text{if } s_0r_0 \text{ well-typed} \quad (FA) \\ (\llbracket a \rrbracket + \llbracket b \rrbracket)^{[0:=r_0s_0]} & \text{otherwise} \quad (BA) \end{cases}$$

For  $t_1[+f_j] = a$  with  $\llbracket a \rrbracket = (s_0, \ldots, s_k)$ , with subtree  $t_2[-f_j]$ ,

$$\llbracket im(a) \rrbracket = \begin{cases} \llbracket a \rrbracket & \text{if } FF(t_2) = -f_i, i = j \quad (ck) \\ \llbracket a \rrbracket^{[0:=some(\lambda x_j. x_i = x_j \land s_0), i:=s_j, j:=\epsilon]} & \text{if } FF(t_2) = -f_i \in L \quad (ck) \\ \llbracket a \rrbracket & \text{if } FF(t_2) \notin L \quad (0) \\ \llbracket a \rrbracket^{[j:=\epsilon, 0:=s_j(\lambda x_j. s_0)]} & \text{if } t_2 \text{ has no features. } (bnd) \end{cases}$$

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