## Class 5: Rule+constraint theories; taking stock

## To do

- Forget about Sommerstein reading on syllabus-get started on Prince \& Smolensky excerpt instead (SQs due Thursday)
- Metaphony assignment is due Tuesday

Overview: First we'll try to make the framework for rule/constraint interaction more explicit. Then, we'll turn to some big-picture issues (reviewing levels of adequacy) and consider some of the questions you've been asked to ponder in your study questions.

1. Implementing triggering: Sommerstein's (1974) ${ }^{1}$ proposal (underlining is mine)
"A P-rule R is positively motivated with respect to a phonotactic constraint C just in case the input to R contains a matrix or matrices violating C and the set of violations of C found in the output of $R$ is null or is a proper subset of the set of such violations in the input to R." (p. 74)
"A rule, or subcase of a conspiracy, positively motivated by phonotactic constraint C does not apply unless its application will remove or alleviate a violation or violations of C." (p. 75)

Later modified: "a rule applies if its application will remove or alleviate a violation of AT LEAST ONE of its motivating constraints" (p. 87)

## 2. Latin example (Sommerstein p. 87)

$$
\begin{aligned}
& \text { genitive sg. nominative sg. UR } \\
& \text { lakt-is lak /lakt/ } \\
& \text { kord-is kor /kord/ } \\
& \left.\left[\begin{array}{c}
+ \text { continuant } \\
<- \text { voice }>
\end{array}\right] \rightarrow \varnothing /\left[\begin{array}{c}
+ \text { consonantal } \\
<- \text {-continuant }
\end{array}\right\rangle\right]-\#
\end{aligned}
$$

positively motivated by two constraints that are surface-true in the language:

| "no final voiced in cluster" | + consonantal $]\left[\begin{array}{c}\text { +consonantal } \\ \text { +voice }\end{array}\right] \#$ |
| :--- | :---: |$]$

paraphrase: if you have a word-final cluster of two obstruents, the second must be coronal, and if the first is a stop the second must be a fricative (/st $\mathrm{ps} \mathrm{ks} /$ are allowed).

- With those constraints, how much can we simplify the deletion rule?

[^0]A derivation might look like this:

| violates no final voiced in cluster? <br> violates final obstruent cluster restrictions? <br> if so, tentatively apply deletion <br> is the violation alleviated/eliminated? <br> if so, accept the change (else don't) | /lakt/ | /kord/ | /re:k |  |
| :---: | :---: | :---: | :---: | :---: |
|  | no | yes | no | we'll have to fill in this part according to how we formulate the rule. |
|  | yes | no | no |  |
|  |  |  | NA |  |
|  |  |  | NA |  |
|  |  |  | NA |  |
|  |  |  |  |  |

Imagine a hypothetical language, "Matin", that is just like Latin except that it has this rule too:

$$
[] \rightarrow \text { [-voice }]
$$

- How does our derivation change? Do we need to add more information to the grammar?

Imagine a hypothetical language, "Natin", that is just like Latin except that it has this rule too:

$$
[] \rightarrow \text { [+continuant }]
$$

- How does our derivation change? Do we need to add more information to the grammar?


## 4. Partial violation, violation alleviation

Under Sommerstein's conception, a constraint doesn't have to be surface-true to be part of the grammar.

The DEGREE OF VIOLATION $\mathrm{V}_{\mathrm{M}, \mathrm{C}}$ to which a matrix M violates a phonotactic constraint C is equal to the cost of the minimal structural change necessary to turn M into a matrix satisfying C.
The application to a matrix M of operation A alleviates a violation in M of phonotactic constraint C just in case the output $\mathrm{M}^{\prime}$ of such application is such that $0<\mathrm{V}_{\mathrm{M}^{\prime}, \mathrm{C}}<\mathrm{V}_{\mathrm{M}, \mathrm{C}}$ (p. 76)

- Can you invent a case where a violation could be alleviated without being eliminated? (It's OK if it's silly-it's hard to think of plausible cases, and Sommerstein himself introduces this idea just to keep the possibility open, not because he has any data that require it.)


## 5. Implementing blocking: taking inspiration from Sommerstein...

A P-rule R is negatively motivated with respect to a phonotactic constraint C just in case the tentative output of R contains a matrix or matrices violating C and the set of violations of C found in the input to R is null or is a proper subset of the set of such violations in the tentative output of $R$.

A rule that is negatively motivated by phonotactic constraint C does not apply if its application will create or worsen a violation or violations of C .

The application to a matrix M of operation A worsens a violation in M of phonotactic constraint $C$ just in case the output $\mathrm{M}^{\prime}$ of such application is such that $\mathrm{V}_{\mathrm{M}^{\prime}, \mathrm{C}}>\mathrm{V}_{\mathrm{M}, \mathrm{C}}$

## 6. What a derivation might look like

| syncope rule | $V \rightarrow C-C$ |
| :--- | :--- |
| cluster constraint | $*\left\{\begin{array}{l}\# \\ C\end{array}\right\} C\left\{\begin{array}{l}\# \\ C\end{array}\right\}$ |

tentatively apply syncope
does this create/worsen violation of cluster constraint?
if not, accept the change (otherwise reject)

| /abito/ | lildoku/ | /uda/ |
| :--- | :--- | :--- |
| (abto) | (ildku) | NA |
| no | yes | NA |
| abto | ildoku | NA |
| [abto] | [ildoku] | [uda] |

## 7. Blocking vs. triggering: Myers 1991's ${ }^{2}$ persistent rules

Zulu: prenasalized affricates, but no prenasalized fricatives. We might propose a constraint: ${ }^{3}$

* $\left[\begin{array}{c}\text { +continuant } \\ + \text { nasal }\end{array}\right]$

Here is a prefix that creates prenasalized consonants (p. 329):

| singular | plural |  |
| :---: | :---: | :---: |
| u:-bambo | izi ${ }^{\text {m }}$ bambo | 'rib' |
| u:-p ${ }^{\text {h }} \mathrm{ap}^{\text {h }} \mathrm{e}$ | izi- ${ }^{\text {m }}$ pap ${ }^{\text {h }}$ | 'feather' |
| ama-t ${ }^{\text {hat }}{ }^{\text {h }} \mathrm{u}$ | ezi- ${ }^{n} \operatorname{tat}^{\text {h }} \mathrm{u}$ | 'three' |
| us-k ${ }^{\text {h }}$ uni | izi- ${ }^{\text {²k }}$ kuni | 'firewood |

- Assume the underlying form of the prefix is /izin/. Formulate a prenasalization rule.

[^1]Here's what happens when the prefix attaches to a fricative-initial stem:

| singular <br> eli-fa | $\begin{aligned} & \text { plural } \\ & \mathrm{e}-\mathrm{n}_{\mathrm{t} f} \end{aligned}$ | 'new' |
| :---: | :---: | :---: |
| u:-fudu | izi- ${ }^{\text {² }}$ - ${ }^{\text {dudu }}$ | 'tortoise' |
| u:-sizi | izi-" ${ }^{\text {Tsizizi}}$ | 'sorrow' |
| u:-zwa | izi- ${ }^{\text {n }}$ ¢zua | 'abyss' |
| u:-zime | izi- ${ }^{\text {n }}$ dzime | 'walking staff' |
| u:-bubu | izi- ${ }^{\text {d }}$ djubu | 'groundnut' |
| u:-Sikisi | izi-" ${ }^{\text {¢ }}$ Sikisi | 'quarrelsome person' |

- What would happen if prenasalization were subject to blocking by the constraint above?

Myers proposes instead a "persistent rule"-it tries to apply at every point in the derivation, so that any time its structural description is created, it immediately gets changed.

$$
\left[\begin{array}{c}
\text { +nasal } \\
+ \text { continuant }
\end{array}\right] \rightarrow\left[\begin{array}{c}
\text { +delayed release } \\
\text {-continuant }
\end{array}\right] \quad \text { i.e., nasal fricative } \rightarrow \text { affricate }
$$

- Let's spell out what the derivation would look like.
- Can we recast this as a simpler rule that is triggered by the constraint?


## Reflecting on big-picture issues

How do humans learn, store, and use linguistic sound patterns? Chomsky lays out a useful framework for investigating this question for language in general (see Chomsky $1965^{4}$ pp. 25-27-but what it is below is an amalgam of various works, slightly simplified and colored by my own views).

[^2]
## 8. Preliminaries

Let a grammar consist of (at least) ${ }^{5}$

- a function that labels any utterance as grammatical or ungrammatical. We can call such labelings grammaticality judgments.
- a function that assigns truth conditions to any utterance

The grammar might be implemented as a lexicon and a list of rules, or a set of constraints, or something else.
Let a linguistic theory be a function that, given a (finite) set of utterances (the learning data), produces a grammar. ${ }^{6}$

These functions should be accompanied by algorithms for calculating them.
Let's use a concrete example, English noun plurals.

| cat | $\mathrm{k}^{\mathrm{h}}$ æt | $\mathrm{k}^{\mathrm{h}}$ ¢ts |
| :---: | :---: | :---: |
| sack | sæk | sæks |
| dog | dag | $\operatorname{dagz}$ |
| grub | gıлb | gııbz |
| dish | dif | difaz |
| fudge | $\mathrm{f} \wedge \overline{\mathrm{d}} 3$ |  |
| pea | $\mathrm{p}^{\mathrm{h}} \mathrm{i}$ | $\mathrm{p}^{\mathrm{h}} \mathbf{i z}$ |
| cow | $\mathrm{k}^{\mathrm{h}}$ au | $\mathrm{k}^{\mathrm{h}} \mathrm{a} u \mathbf{z}$ |
| man | mæn | men |
| foot | fut | fit |
| wife | waif | waivz |
| whiff | wif | wifs |

## 9. Observational adequacy

A grammar that accepts all the forms that a typical speaker would have been exposed to and assigns the right truth conditions to them (we don't care what the grammar says about other forms), is an observationally adequate grammar.

Note that there are infinitely many observationally adequate grammars for any (finite) set of learning data (why?).

[^3]Examples of observationally adequate grammars for English noun plurals
I. (just list every word you know)

| $\mathrm{k}^{\text {h }}$ ¢ | $\mathrm{k}^{\mathrm{h}}$ ¢ts | dif | dif $\mathrm{d}^{\text {z }}$ |
| :---: | :---: | :---: | :---: |
| sæk | sæks | $\mathrm{f} \wedge \overline{\mathrm{d} 3}$ |  |
| dag | $\operatorname{dag} \mathbf{z}$ | $\mathrm{p}^{\mathrm{h}} \mathrm{i}$ | $\mathrm{p}^{\mathrm{h}}$ iz |
| gıлb | gııbz | $\mathrm{k}^{\mathrm{h}}$ au | $\mathrm{k}^{\mathrm{h}} \mathrm{a} u \mathrm{z}$ |

mæn men
fut fit
waif waivz
wif wifs
I.e., the grammar's judgment function accepts utterances containing those items in positions where a plural is required (I like cats); its truth-condition-assigning function assigns the appropriate truth-conditions to utterances containing the items in the right column (I like cats is true iff I like members of the cat group-it has nothing to do with whether I like members of the dog group).
II. Add -s to everything, except for these exceptions:

| dag dagz | $\mathrm{f} \wedge \overline{\mathrm{d}} 3$ |  | mæn | men |
| :---: | :---: | :---: | :---: | :---: |
| gıлb gıл ${ }^{\text {did }}$ | $\mathrm{p}^{\mathrm{h}} \mathrm{i}$ | $\mathrm{p}^{\mathrm{h}} \mathbf{i z}$ | fut | fit |
| dif difaz | $\mathrm{k}^{\mathrm{h}} \mathrm{au}$ | $\mathrm{k}^{\mathrm{h}} \mathrm{auz}$ | waif | waivz |

III. Add -z to everything, except for these exceptions:
$\mathrm{k}^{\mathrm{h}} \mathfrak{\mathrm { k }}{ }^{\mathrm{h}} \mathfrak{\mathrm { t }}$,
sæk sæks
dif difaz
$f \wedge \overline{d 3} \quad f \wedge \overline{d 3} \partial z$
mæn men
fut fit
waif waivz
wif wifs
IV. Add $-\partial z$ after "sibilant" sounds, -s after non-sibilant [-voice] sounds, and $-z$ otherwise, except for these exceptions:
mæn men
fut fit
waif waivz
IV. Change final /f/ to [v], and then add -az after "sibilant" sounds, -s after non-sibilant [voice] sounds, and $-z$ otherwise, except for these exceptions:

| mæn | men |
| :--- | :--- |
| fut | fit |
| wif | wifs |
| $\ldots$ | $\ldots$ |

## 10. Descriptive adequacy

A grammar that not only is observationally adequate, but also gives the same treatment to novel utterances that a real speaker of the target language gives is a descriptively adequate grammar.

The idea is that a descriptively adequate grammar captures the generalizations that real learners extract from the learning data-I think it makes the most conceptual sense to operationalize this in terms of novel utterances.

In a famous early study of children, Berko $(1958)^{7}$ found that English-speaking adults (all highly educated, in her sample, FWIW) consistently give the following plurals when presented with invented words (pp. 155-158):

| W $\wedge$ g | W $\wedge$ gz | $1 \wedge n$ | $1 \wedge n z$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{g} \Lambda \widetilde{\mathrm{tf}}$ | $\mathrm{g} \Lambda \widetilde{\mathrm{t}} \boldsymbol{\partial z}$ | nIZ | nIZəz |
| kæ3 | kæろəz | kıa | k.ıaz |
| to. | to.lz | tæs | tæsəz |

- Which of the grammars above could be descriptively adequate, given these data?
- The adults disagreed about this word-what might we conclude?
heaf hifs, hivz


## 11. Descriptive adequacy is hard!

Achieving descriptive adequacy is often spoken of as though it were easy or could happen through inspection of basic data, but under Chomsky's definition it is actually a huge challenge.

Words that the speaker already knows are uninformative! (They don't tell us anything about what generalizations the speaker has learned-she may have simply memorized that word.)

Constructing novel phonological situations to put speakers in is difficult. Contrast this with syntax, where it's easy to construct sentences that-presumably-the speaker has not encountered before.

- Remember the K\&K discussion of Russian devoicing. They point out some observationally adequate accounts that don't include a rule of final devoicing:
- list two allomorphs for the stems that alternate (/...b/\&/...p/ vs. /...p/ for stems that don't alternate)
- have a devoicing rule but characterize the environment in morphological terms (e.g., "end of nominative singular") instead of /__\#
- have separate rules for $\mathrm{b} \rightarrow \mathrm{p}, \mathrm{d} \rightarrow \mathrm{t}$, etc.

They had some arguments that these accounts are not descriptively adequate. You were asked to consider those arguments' satisfactoriness. So what do you think?

[^4]
## 12. Explanatory adequacy

A theory that, when given a typical set of learning data, returns a grammar that is descriptively adequate, is an explanatorily adequate theory.

Obviously, developing an explanatorily adequate theory is a huge challenge!


[^0]:    ${ }^{1}$ Sommerstein, Alan H. (1974). On Phonotactically Motivated Rules. Journal of Linguistics 10: 71-94.

[^1]:    ${ }^{2}$ Myers, Scott (1991). Persistent rules. Linguistic Inquiry 22: 315-344.
    ${ }^{3}$ Myers actually uses autosegmental representations.

[^2]:    ${ }^{4}$ Chomsky, Noam (1965). Aspects of the theory of syntax. Cambridge: MIT Press.

[^3]:    ${ }^{5}$ We probably want the grammar to do much more. It could, given an utterance, return a gradient "goodness score" rather than a simple binary judgment. Given one utterance and some instruction, it could return some other utterance (e.g., cat + PLURAL $=$ cats). And of course there's a lot more to meaning than truth conditions. (Chomsky also requires a grammar to assign a structural description to an utterance, but I wonder if this is begging the question: the structural description can be used to explain more-observable properties of a sentence like its truthconditions, but we don't know a priori that it's necessary.)
    ${ }^{6}$ Chomsky's definition of a linguistic theory is weaker: it need only define the set of possible grammars, independent of learning data. This allows Chomsky to define the term descriptively adequate theory, which is a theory that includes, as possible grammars, a descriptively adequate grammar for every language-but does not necessarily return that grammar given learning data for that language.

[^4]:    ${ }^{7}$ Berko, Jean (1958). The child's learning of English morphology. Word 14: 150-177.

