

**Class 18 (Week 9, T)**  
**Induction I: constraints**

**To do**

- Work on your project! (There's no more homework and no more reading.)
- There is no class on Thursday (Thanksgiving)
- Next Tuesday we meet **4-6 PM**, in **Campbell 2122** (conference room)

**Overview:** What if we aren't born with a constraint inventory? We'll take a tour of some proposals.

**1. Discuss Hayes & Wilson (2006)**

**2. Naradowsky, Pater & Smith (2011): Error-driven constraint induction**

- Do we really need to consider such a broad range of constraints?
- Main idea:
  - When you hear a form (say, [#n...]), compare it to a randomly sampled, hypothetical similar form (e.g., [#ŋ...])
  - If your current grammar assigns better harmony to the sampled neighbor than to the observed form, the grammar needs updating
    - Can you see a problem with this?
  - Refinement: remember the last  $n$  forms you heard (here,  $n=3000$ ), and don't worry about a neighbor that's in that set
- How to construct a constraint
  - Make a lattice of all the constraints that could prefer the observed form
    - In the [#n...]/[#ŋ...] example, consider all constraints that penalize [+dorsal]
      - In the feature system used in this paper, [CORONAL] is privative
        - Which means what?
      - Let's draw some of the lattice.
  - Sample a few of these constraints (here, 3) and add them to the grammar
  - Update weights of this new constraint set
    - Use Perceptron rule to update: similar to Gradual Learning Algorithm, except it cares about the number of violations
- More precisely: see over

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**Algorithm 1** Learning Procedure
 

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1: function LEARN
2:   model  $\leftarrow$  []
3:   while learning do
4:      $o \leftarrow \text{draw}(D)$ 
5:      $u \leftarrow \text{draw}(\text{neighborhood}(o))$ 
6:     if model.score( $u$ ) > model.score( $o$ ) then
7:        $\text{diff} \leftarrow u.\text{features} \setminus o.\text{features}$  ▷ Constraint Induction
8:        $\text{cspace} \leftarrow []$ 
9:       for  $c \leftarrow \text{allconstraints}$  do ▷ Filter Space
10:        if  $c.\text{contains}(\text{diff})$  then
11:           $\text{cspace}+ = c$ 
12:        end if
13:        model.features+ =  $\text{draw}(\text{space})$  ▷ Add constraint
14:      end for
15:      for  $j \leftarrow 0$  until model.size do ▷ Perceptron Update
16:        model[ $j$ ] =  $f.\text{violations}(u) - f.\text{violations}(o) * \text{rate}$ 
17:      end for
18:    end if
19:  end while
20: end function
21:
22: function NEIGHBORHOOD( $o$ )
23:    $\text{plattice} \leftarrow [o.\text{size}]$ 
24:   for  $i \leftarrow o.\text{size}$  do
25:      $\text{plattice}[i] \leftarrow o[i].\text{phones}$  ▷ (Phone, Distance) pairs
26:   end for
27:   return  $\text{draw}(\text{plattice.allPaths})$  ▷ Sum weight in each path
28: end function

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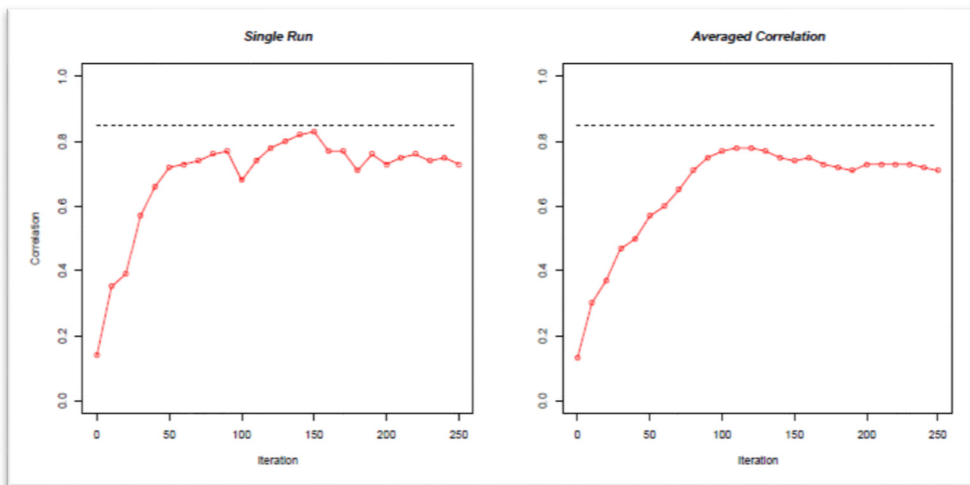
(p. 13)

- Tested on English onsets, as in Hayes & Wilson (2006)
- Resulting constraints (over):
  - [ ] means “any segment”, i.e. [+segmental]

Weight	Feature	Description
1.34	[ <sup>-</sup> [-strid,+cor]	S T vs. TH S
1.28	[ <sup>+</sup> +cons,+ant]	S vs ZH
1.26	[ <sup>-</sup> -approx,+lab]	M vs. NG
1.26	[ <sup>-</sup> [-cons,+cor]	G R vs. P W
1.26	[-approx,-voice] [ <sup>-</sup> -ant,+cor]	G R vs. CH L
1.22	[ <sup>-</sup> -son,-voice] [ <sup>-</sup> ]	S K vs. Z P
1.22	[ <sup>+</sup> +strid][-strid,+son]	S L vs TH L
1.20	[ <sup>-</sup> -son,+voice][+lab]	G R vs. P W
1.20	[ <sup>+</sup> +dorsal,+cons][ <sup>+</sup> +approx,-ant]	G R vs. P W
1.20	[ <sup>+</sup> +dorsal][ <sup>-</sup> -strid,-ant]	G R vs. CH L
1.18	[ <sup>+</sup> +cont,-voice]	S vs. ZH
1.18	[+strid,+cor][ <sup>-</sup> -strid]	S T vs. S S
1.18	[-son,-voice][ <sup>-</sup> ]	G R vs. P W
1.18	[ <sup>-</sup> ][ <sup>+</sup> +approx,+cor]	G R vs. P Y
1.16	[-son,+ant][-ant]	S W vs. S R
1.16	[ <sup>-</sup> ][ <sup>+</sup> +high,+approx]	S W vs. S R
1.16	[ <sup>-</sup> ][ <sup>+</sup> +high,+son]	S W vs. S R
1.16	[ <sup>-</sup> -voice][ <sup>-</sup> ]	T R vs. V R
1.14	[ <sup>+</sup> +strid,-voice][ <sup>-</sup> ]	S L vs. TH L
1.14	[-son][ <sup>+</sup> +ant,+lat]	S L vs. S R

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- Correlation to human judgments of English onsets: -0.829 (vs. Hayes & Wilson’s -0.859)
- Interesting problem: tendency towards over-fitting as learning continues
  - As assessed by worsening correlation to human judgments



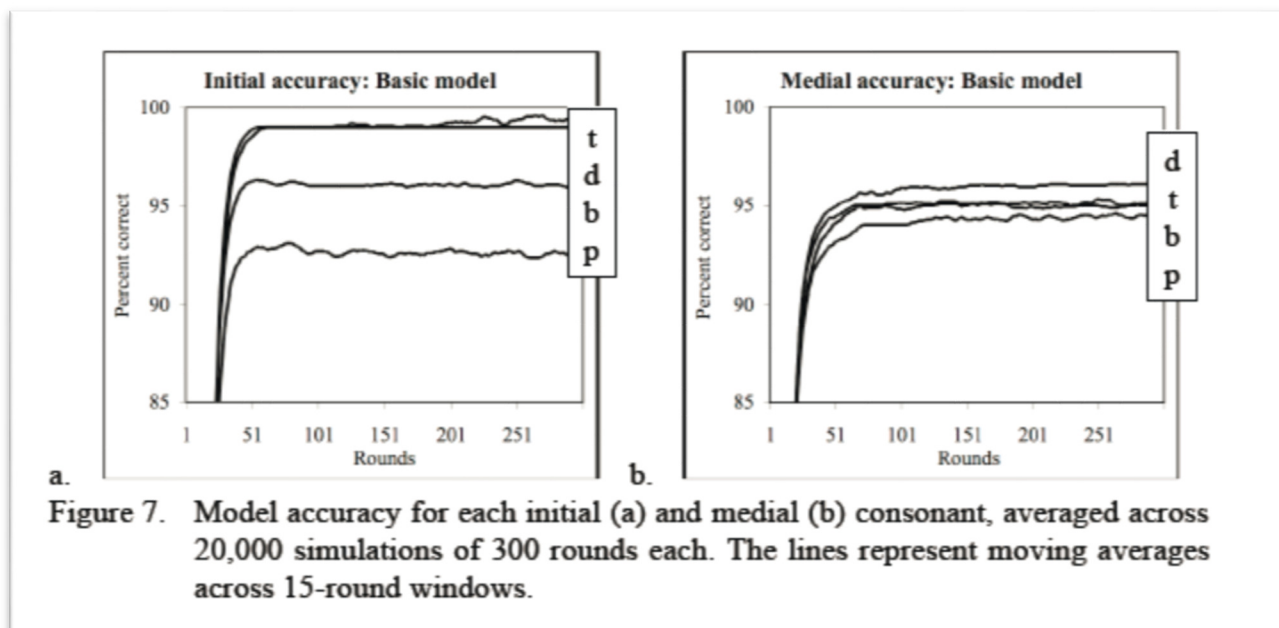
(p. 18)

- See the paper for some ways to improve the model
- Discuss: Both this model and the Hayes/Wilson model are for phonotactic learning. How could we extend either of these to learning alternations?

### 3. Flack (2007): inducing a constraint from perceptual experience

We got this far.

- There are languages that prohibit [p] specifically in word-initial position: \*#P
  - Initial [p] has particularly short VOT, and it's more variable than initial [b]'s
  - Difference in maximum burst intensity for initial [p] and [b] is smaller than for other voiceless-voiced pairs (p. 122)
- To produce an instance of a category ([p], [b], [t], etc.) in a context, speaker samples values for various phonetic dimensions from stored distributions centered on prototype
- In perception, listener must guess the category
  - Some noise is added: perception is imperfect
  - Rather than Bayes' rule as in Kirby (2013), finds the closest prototype
- Listener gets feedback on accuracy
  - Allows listener to update prototypes
  - Listener also **stores accuracy rate** for each category, perhaps over a moving window of the past  $n$  tokens (here,  $n=400$ )
    - Specifically, **hit rate** and **false alarm rate**
  - Does anyone know these terms?
- Hit rates for each consonant as learning proceeds over time:



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- Important point about phonologization
  - Once \*#P has been promoted high enough, the learner gets no experience of initial [p]!
  - But they do still have one important piece of information listed above—can you guess what?

- The learner's rule for inducing a constraint:

(117) Some segment  $x$  is perceptually difficult in some context  $Context_Z$  if either:

a.  $Accuracy(x/Context_Z) < threshold$

and

$Accuracy(x/Context_Z) < Accuracy(y/Context_Z) \rightarrow Constraint *x/Context_Z$

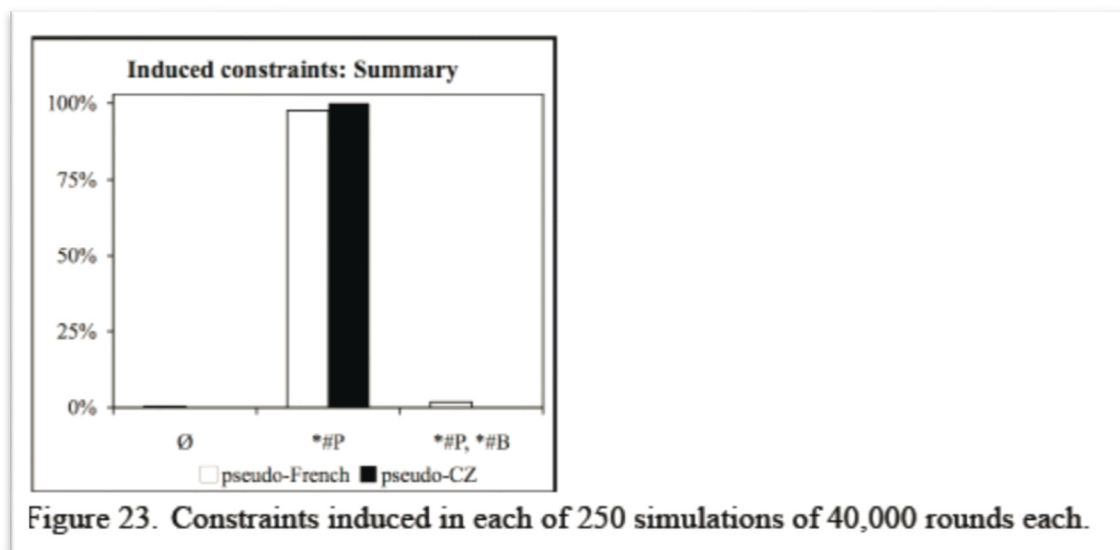
This difference must be significant ( $\alpha = 0.01$ ).

b.  $Accuracy(x/Context_Z) < FalseAlarm(x/Context_Z) \rightarrow Constraint *x/Context_Z$

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- Where “accuracy” means hit rate
- If there is no hit rate, because the sound never actually occurs in that context, treat it as 0.
- So how would this work for a language with no initial [p]? Let's draw a possible confusion matrix.

- Results: both a learner of simplified French (has initial [p], but it is perceptually difficult) and a learner of simplified Cajonos Zapotec (no initial [p]) learn  $*\#P$  in nearly all runs



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#### 4. A selection of other approaches that we won't have time to cover in depth

- Hayes (1999): as we saw last time, generate lots of features according to a set of templates, and then select the ones that match the phonetic map well, with a bias favoring simpler constraints
- Boersma & Pater (2007): in Harmonic Grammar, construct *positive* constraints for every property that the observed form has (as well as some other constraints, including negative ones)
  - e.g., on observing Canadian English [ʔΛIS] 'ice', construct these, among many others:

(17) *Observed structure*                      *Constructed constraint*

a.        D    RAISED DIPHTHONG: A diphthong must be [-low]  
           [-low]                                        (Assign a reward of 1 to each diphthong that is [-low])

b.        D    C                                        RAISED/VOICELESS: A diphthong preceding a voiceless  
           [-low][-vce]                                consonant must be raised  
     (Assign a reward of 1 to each diphthong that is [-low] that  
     precedes a voiceless consonant)

(p. 4)

- Pater (2014) proposes something similar for the same case, but now without positive constraints
- Moreton (2010): explore infinite space of possible constraints with evolutionary algorithm
  - Every subpart of every possible representation is a constraint
  - Start with a random set of constraints
  - Error-driven: if current grammar selects a candidate that doesn't match the observed true winner...
    - constraints that favor observed forms (correct winners) are allowed to breed.
    - breeding = combine two constraints to produce a new, offspring constraint with aspects of each parent. Offspring can also mutate.
- Pizzo (2013): Inducing constraints to handle alternations (Turkish vowel harmony and devoicing)
  - On making an error, create a constraint at random
  - According to certain templates
  - Can be faithfulness or markedness
  - Must penalize some way in which the spurious winner differs from the observed winner
  - The researcher can set parameters for how much stem-faithfulness and tier-markedness constraints show be allowed/favored
- Alderete, Tupper & Frisch (2013): Connectionst model of OCP-Place in Arabic roots

#### 5. Coming up next Tuesday (there is no class this Thursday)

- Inducing feature and natural classes

**References**

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