

## Additive markedness interactions in phonology

### 1 Markedness thresholds and cumulative constraint interactions

(1) A common intuition: rules/constraints evaluate strings independently

- Each rule/constraint has a structural description
  - #CC (initial clusters)
  - $\left[ \begin{array}{c} -\text{son} \\ +\text{voi} \end{array} \right] \left[ \begin{array}{c} -\text{son} \\ +\text{voi} \end{array} \right] \#$  (final clusters of voiced obstruents)
- Violation/application is triggered whenever structural description is met, regardless of what occurs elsewhere in the word
- Not observed, in English or elsewhere (?)
  - Final /bd/ repaired by epenthesis only if there are multiple voiced clusters in the word: [ɹʌbd] ‘rubbed’, but [əbzɔɹbəd] ‘absorbed’
  - Final /bd/ repaired by epenthesis only if the word has an onset cluster: [ɹʌbd] ‘rubbed’, but [gɹæbəd] ‘grabbed’
- If a structure is tolerated, it is tolerated regardless of violations elsewhere in the word
  - No ‘markedness threshold’ beyond which structures suddenly become intolerable

(2) A surprising pattern: Lakhota (Siouan)

- Roots may contain a wide variety of structures, including fricatives, aspirated/ejective obstruents, and consonant clusters
- However, unexpectedly few roots with combinations of these structures
  - Two clusters (*gleʃka* ‘spotted’, *wiktʃemna* ‘10’)
  - Two fricatives (*fofa* ‘bubbly’)
  - Cluster + aspirate/ejective combinations (*x’akpa* ‘curved/ruffled’, *bleʃ<sup>h</sup>a* ‘decline in health’)
  - Cluster + fricative combinations (*mnuya* ‘crunch on’)
- Cumulative effect: multiple marked structures interact to make word less likely

(3) A similar phenomenon in English (other examples below)

- English allows initial #Cl clusters (*clip*, *black*) and final sC# consonant clusters (*list*, *lisp*, *risk*)
- However, unexpectedly few words combining #Cl and sC#
  - Just two in CELEX: *blast*, *clasp* (\**glisp*, \**clesk*, \**ploast*, \**flisk*, ...)
- Gradient restriction: morphemes can end in sC] unless there’s a [Cl onset

(4) Claims of this talk

- Cumulative phonological restrictions: combinations of independently dispreferred structures are worse than expected
- A gradient (statistical) effect (not a categorical ban on combinations of otherwise perfectly acceptable structures)

- A static phonotactic effect (no alternations when violations are created through affixation)
  - Lakhota: *x'an-kte* 'work-FUT'
  - English: *glossed* [glɒst], *placed* [pleɪst] (\*[glɒsəd], \*[pleɪsəd])
- These effects, and the observed restrictions, can be derived with a model in which...
  - Candidates compete according to the sum of their weighted violations
  - A 'threshold' constraint imposes a markedness cutoff on acceptability of words to derive static phonotactic patterns

#### (5) Outline

- Demonstrating the effect: a lexical study of Lakhota
- The weighted constraint model: schematic illustration
- Applying the model: learning a grammar from the Lakhota lexicon
- Parallel example from English (with evidence about native speaker intuitions)
- Residual issues...

## 2 Cumulative markedness interactions: Lakhota

### 2.1 The basic pattern

#### (6) Background on Lakhota (Siouan)

- Stops and affricates: three-way contrast
 

		Initial		Medial	
Voiceless unaspirated	p, t, tʃ, k	ka	'there'	ʃaka	'strong'
Aspirated	p <sup>h</sup> , t <sup>h</sup> , tʃ <sup>h</sup> , k <sup>h</sup>	k <sup>h</sup> a	'to mean'	māk <sup>h</sup> a	'earth'
Ejective	p', t', tʃ', k'	k'a	'to dig'	tʃik'ala	'small'
- Fricatives: similar three-way contrast
 

		Initial		Medial	
Voiceless	s, ʃ, x, h	xã	'scab'	ixa	'to laugh'
Voiced	z, ʒ, ʁ	ɣã	'messy hair'	hoɣã	'fish'
Ejective/glottalized	s', ʃ', x'	x'ã	'to do'	ptux'a	'to crumble'
- Sonorants: m, n, l, w, j

#### (7) Syllable structure

- Syllables generally of the form C(C)V
- Extensive set of CC onset clusters
  - Unaspirated stop + sonorant: *blo*<sup>1</sup> 'potato', *gmū* 'twisted'
  - Unaspirated stop + obstruent: *kju* 'to bead', *ksapa* 'wise', *kte* 'to kill', *tka* 'heavy'
  - Fricative + C: *spã* 'to thaw', *xʃã* 'to bloom', *xmū* 'to buzz', *flo* 'to melt'
  - Nasal + nasal: *mni* 'water'

#### (8) Root shape

- Lakhota words can become quite long through affixation
 

<i>wa-</i>	<i>ju-</i>	<i>o-</i>	<i>ki-</i>	<i>wãzi-la</i>	'unite'
	indef. obj.-causation-loc.-to/for-one-		dimin.		

<sup>1</sup>Unaspirated stops become voiced before sonorants in clusters (and a short epenthetic vowel is typically inserted: [b<sup>ɔ</sup>lo]).

- Clusters, fricatives, ejectives, etc., are mostly found in roots, which are often quite short
  - $C_0V$ ,  $C_0VC(V)^2$ ,  $C_0VC_0V$
  - Longer monomorphemic roots: *payōta* ‘duck’, *wagmiza* ‘corn’, *it̃jamna* ‘snow’
  - However, long roots frequently behave as if they are morphologically complex (e.g., other morphemes are ‘infix’d in the middle of them, or other words with shared pieces and vaguely related meanings; for discussion, see Boas and Deloria 1941, pp. 26–28)
- Affixes (especially, prefixes) tend to use simple syllable structure, unmarked segments (sonorants, voiceless unaspirated stops, voiceless fricatives)—e.g.,

Locative	<i>o-</i> , <i>i-</i> , <i>a-</i> , ( <i>e-</i> ), <i>ki-</i>	Causative	<i>-ja</i> , <i>-k<sup>h</sup>ija</i>
Valence	<i>wa-</i> , <i>a-</i> , <i>ki-</i>	Tense	<i>-hā</i> , <i>-s’e</i> , <i>-kte</i>
Manner	<i>ka-</i> , <i>na-</i> , <i>pa-</i> , <i>ja-</i> , <i>ju-</i>		
Person markers	<i>wa</i> , <i>ja</i> , <i>ū(k)</i> , <i>ma</i> , <i>ni</i> , <i>tʃ<sup>h</sup>i</i> ; reflexive <i>-it̃ʃ<sup>h</sup>i-</i>		

- Reduces the probability of encountering multiple clusters, ejectives, etc., in a word
  - Plausibly attributed to the morphological structure of words + phonological restrictions on affixes, not a ban on multiple clusters/fricatives/etc.

☞ Restrictions are most interesting within roots, where marked structures are freely allowed

(9) Within roots: statistically gradient cooccurrence restrictions

- Carter (1974, p. 51): general restriction of one cluster per morpheme
  - Many words like *ksapa* ‘wise’, *igmu* ‘cat’
  - Few words like *gleʃka* ‘spotted’, *wikt̃jemna* ‘10’
- Informal observation suggests that roots with two fricatives are also scarce
  - Lots of words like *kaye* ‘to make’, *sapa* ‘black’, *ɣopa* ‘snore’
  - Few words like *xuya* ‘dent’, *sofa* ‘bubbly’
  - Virtually no words like \**ɣofa* (distinct fricatives)
- Combinations of fricatives with clusters are also rare
  - A few cluster-first examples: *mnuya* ‘eat crunchily’, *ʃloya* ‘make hominy’
  - Very few fricative-first examples: *ɣoptā* ‘listen’, *ʃakpe* ‘six’
- Roots with ejective + cluster combinations also rare
  - Few words like *ptux’a* ‘crumble’

## 2.2 A lexico-statistical study

(10) The Lakhota lexicon

- Constructed database of 12,396 entries in Buechel and Manhart (2002) dictionary
  - All entries except those beginning with *a-*, *i-*, *o-* (omitted since mostly prefixed, and could be left out without systematically undercounting any particular class of consonants)
- Rough morphological parsing to identify roots
  - Separated recurring roots and prefixes (distributional criterion)
  - Used meaning as a check to reduce hyperanalysis
 

*hoγā* ‘fish’ ≠ *ho+γā* ‘bushy+voice’; *t<sup>h</sup>aspā* ‘apple’ ≠ *t<sup>h</sup>a+spā* ‘thaw+ruminant’s body part’

<sup>2</sup>There is a set of roots that are sometimes analyzed as /C<sub>0</sub>VC/, but which always surface with a final vowel; see Shaw (1980) for discussion.

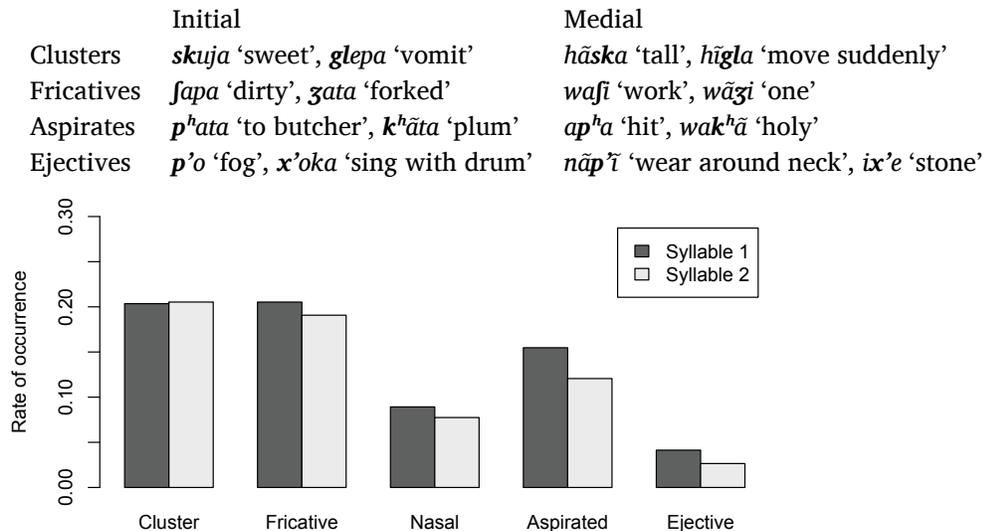
- Extracted mono- and di-syllabic morphemes
  - Removed reduplicated and contracted forms (show independent phonological restrictions)
  - Removed allomorphs derived by final vowel changes ('ablaut')
  - Removed morphemes longer than 2 syllables, as more likely to be complex or misanalyzed
  - Result: 2,275 entries (351 monosyllabic, 1924 disyllabic)
- Caveat: many entries that are almost certainly morphologically complex remain un-decomposed, and some words probably also over-decomposed
  - Less of a problem in 1–2 syllable morphemes, which we focus on here
- One other caveat: marking of aspiration in dictionary appears to be incomplete, especially for certain segments in initial position (e.g., [tʃ] vs. [tʃʰ])
  - I omit counts of aspirated stops in initial position

(11) Expected rates of occurrence for 'doubly marked' roots

- The question of interest: how often do we see roots that combine marked structures?
- Baseline (independence model):
  - $\text{Prob}(C'VCCV) = \text{Prob}(\text{initial } C') \times \text{Prob}(\text{medial } CC)$
- Are marked structures already expected to be rare in medial position due to positional restrictions?

(12) Positional effects within roots: very weak

- Clusters, fricatives, aspirated stops/affricates, and ejectives can all occur in either initial or medial position



- Nasals look rather infrequent when counted this way, but only 2 nasals, compared with 4 ejectives, 4 aspirates, 6 fricatives, and numerous clusters...
- Clusters, fricatives, nasals, aspirated/ejective stops are not appreciably rarer in medial position
- Thus, we expect that a reasonable number of disyllabic roots should have these structures in both positions simultaneously

## (13) Characterizing the pattern informally: Observed/Expected counts

- Calculated rate of occurrence of consonant types in initial syllable (monosyllables and disyllables together) and second syllable (disyllables only)
  - E.g., clusters in first  $\sigma = 20.4\%$  probability, fricatives in second  $\sigma = 19.0\%$  probability
  - Joint probability = 3.9%
- Expect 75 CCVSV words in a lexicon of 1924 disyllables
- Only 45 CCVSV words actually occur
- O/E = 45/75 = .60 (somewhat underattested)

## (14) Results

Initial	Medial Cluster		Fricative		Aspirated		Ejective	
Cluster	43/80	? 0.54	45/75	? 0.60	11/47	*? 0.23	1/10	*? 0.10
Fricative	43/81	? 0.53	54/75	? 0.72	13/48	*? 0.27	10/10 =	✓0.96
Ejective	5/16	*? 0.31	13/15 =	✓0.86	0/10	* 0.00	8/2 =	3.80

## (15) Restriction on cluster+cluster combinations (Carter 1974)

- Expect: 80 (20.4% in first syllable, 20.5% in second syllable)
- Actual: 43 (O/E = .54)
- 24 of the examples involve pseudoreduplication, and should perhaps be treated separately
  - *glegle, gligla, gmigma, gnāgnā, kpakpa, kpikpi, kpukpa, ktokta, kfikfa, kfikfā, psīpsī, ptepte, pšapša, skiska, stasta, stusta, xtʰaxtʰa, xpaxpa, xpixpi, xwaxwa, xwuxwu, škaškā, škiška, štušta,*
- 19 distinct CC: *blaska, blaski, bluška, glamni, glapšū, gleška, gluštā, gnaška, ktʰāpta, kpanni, pšexte, pšextī, skokpa, skumna, skuxya, slitka, škokpa, škāgle, šteгла*
- Effect may be stronger than O/E value suggests, with numerous exceptions through reduplicative correspondence (Zuraw 2002)
- An OCP(cluster) effect?
  - Not easy to formulate, given standard assumptions about the kinds of structures that OCP constraints penalize (Suzuki 1998)
  - Also, as we are about to see, would be insufficient to capture range of restrictions
- Claim: a cumulative interaction between the individual clusters involved
  - Two violations in *gleška* worse than sum of individual violations in *glepa, škata*
  - Such words are correspondingly rarer than expected

## (16) Fricative-fricative combinations

- Expect: 75 (20.5% in first syllable, 19.0% in second syllable)
- Actual: 54 (O/E = .72)
- 44 of these involve exact or close copies (pseudoreuplicated)
  - *šafte, šikšī, škaškā, škiška, šofa, štušta, šufka, ŷīye, ŷōya, ŷūya, kfikfa, kfikfā, pšapša, psīpsī, psūsū, sasa, sāsā, sisa, sīsī, sīsī, skiska, stasta, stusta, sūsū, xaxa, x'ax'a, xāxā, x'āx'ā, xaxe, xaxla, xexe, x'ex'e, x'ex'e, xlayā, xloyā, xloye, xloyu, xmiŷya, xniya, xpaxpa, xpixpi, xuxa, xwaxwa, xwuxwu*

- Only 10 items with truly distinct fricative-fricative combinations (and most involve a cluster)
  - *ʃix'ā, psexte, psexti, sekse, skuxya, ʃixti, ʃixti, ʃtaxe, xefma, xtfāya*
- An OCP constraint on fricatives? (\*[+cont]...[+cont])
  - Not a commonly observed OCP effect (cf. place, laryngeal features)
  - In fact, this would be the only clear-cut documented case that I'm aware of
  - Positing OCP([+cont]) predicts (wrongly?) languages in which fricatives become stops if there's a fricative earlier in the word
  - Positing OCP([+cont]) also predicts that fricatives specifically dislike cooccurring with other fricatives; we'll see below that this isn't sufficient
- Claim: cumulative effect of two \*Fricative violations

## (17) Fricative-cluster combinations

- Expected: 156 (75 CCVSV, 81 SVCCV)
- Actual: 88 (45 CCVSV, 43 SVCCV) ⇒ O/E = .56
- Interaction of two distinct structures—not an OCP effect!
  - ...and no particular reason to think that there is a \*CC...S or \*S...CC constraint that specifically bans cluster+fricative combinations
- Can only be interpreted as cumulative interaction of constraints against clusters and fricatives

## (18) Not all combinations are underattested

- Ejective-ejective combinations are overattested
  - However, nearly all pseudoreuplicated (*s'is'i, x'āx'ā, t'it'i, k'ik'ik'i, t'it'it'i*, etc.)
  - Otherwise, near total ban on two aspirates/ejectives (MacEachern 1999; Gallagher 2010)
- Ejective-fricative combinations also overattested (will not say more about these here)

## (19) A more rigorous test of the effect: a statistical model of the Lakhota lexicon

- Made a schematic version of the Lakhota lexicon, representing counts of 'major root shapes'
  - Took all 2,275 monosyllabic and disyllabic roots
  - Collapsed segments by place, manner: Stop (T), Fricative (S), Nasal (N), Lateral (L), Glide (J), h, Vowel (V)
    - E.g., *ʃic'e, ʃok'i, ʃic'i* ⇒ SVT'V; *hifma, huxni* ⇒ hVSNV
  - Ignored aspiration on [tʰ] (contrast not marked systematically in dictionary, and aspirated [tʰ] appears not to pattern with other aspirates)
- For each of the 257 resulting root shapes, calculated number of occurrences in the lexicon

## (20) Questions to test

- Can we predict how many times a given root shape occurs in the lexicon, based on the probability of the structures it contains (clusters, fricatives, aspirates, etc.)
- Do predictions improve if we allow additional penalties for combinations of marked structures?
- Approach: nested log-linear models, predicting rates of attestation of different root shapes based on the number of violations of different constraints
  - Start with 'simple' constraints (\*Fricative, \*Aspirate, \*Ejective, \*Nasal, various \*CC)
  - Then, add constraints on combinations to see whether they offer significant improvement (likelihood ratio test)

(21) Baseline model: different classes have different frequencies

Constraint	Coefficient	Sig. ( $\chi^2$ )	Constraint	Coefficient	Sig. ( $\chi^2$ )
*Ejective	-1.434	<.0001	*CC:stop+stop	-1.634	<.0001
*Lateral	-0.941	<.0001	*CC:stop+nasal	-1.233	<.0001
*Nasal	-0.821	<.0001	*CC:stop+liquid/glide	-1.249	<.0001
*Aspirate	-0.693	.012	*CC:fric+stop	-0.421	<.0001
*Fricative	-0.546	<.0001	*CC:fric+liquid/glide	-0.392	<.01
*Glide	-0.191	<.0001	*CC:fric+nasal	-0.098	.511
*Stop	0.459	<.0001			

- Negative coefficient means fewer roots containing the structure in the lexicon

(22) Doubly marked roots, part 1: two of the same structure

- Added constraints for \*CC...CC, \*S...S, \*C<sup>h</sup>...C<sup>h</sup>, \*C'...C', \*N...N
- Likelihood ratio test shows significant improvement over baseline model (p<.0001)
- Specific effects

Constraint	Coefficient	Sig. ( $\chi^2$ )	Constraint	Coefficient	Sig. ( $\chi^2$ )
*CC...CC	-0.852	<.0001	*C'...C'	0.433	0.24
*S...S	-0.517	<.0001	*C <sup>h</sup> ...C <sup>h</sup>	0.608	<.05
*N...N	-0.058	0.83			

- Combinations of two clusters, two fricatives underattested (with stronger effect for clusters)
- Nasals cooccur as often as expected (no additional effect)
- \*C'...C' and \*C<sup>h</sup>...C<sup>h</sup> are surprisingly *overattested*
  - As noted above, virtually all pseudoreuplicated

(23) Doubly marked structures, part 2: distinct structures

↓C1/C2→	*CC	*Fric	*Asp
*Fric	-0.401 ***		
*Asp	-0.546 ***	-0.830 ***	
*Ejec	-0.980	0.344 **	-1.241 **

- Confirms cline of underattestation observed informally above with O/E counts

(24) Summary so far: combinations of dispreferred structures are even rarer than expected

- Degree of underattestation is correlated with frequency of the parts
- Clusters and fricatives show moderate restrictions
  - Lowish frequency in Lakota in spite of large inventories
  - Also cooccur with themselves and with each other somewhat less often than expected
- Aspirates and ejectives show stronger restrictions
  - Clusters and fricatives cooccur with aspirates rather rarely
  - Clusters cooccur with ejectives even more rarely
- Strongest effect: cooccurrence of ejectives with aspirates
  - May also be due to a more general ban on laryngeal cooccurrence

Important: underattestation goes beyond what is expected based on joint probability of the parts!

(25) Maybe we have the wrong expectations?

- Simple expectation: probability of cooccurrence  $AB = \text{joint probability (Prob(A)} \times \text{Prob(B))}$
- Frisch (1996, pp. 152–153): combinations of high frequency elements are likely to be attested, and support learning (or creation?) of additional words containing those combinations
- Combinations of low frequency elements are low frequency, and may even be accidentally unattested, so ‘never get their foot in the door’ (less support for creating )
- Rich get richer and poor get poorer effect → warping such that low expected frequency leads to even lower attested frequency. Perhaps that is all we’re seeing here?

(26) Comparison: cooccurrence with nasals

- Nasals are relatively infrequent in initial position ( $\approx 9\%$ )
- Combinations involving nasals are correspondingly rare, but not unexpectedly so

Initial	Medial Cluster	Fricative	Aspirated	Ejective
Nasal	27/35 = $\checkmark 0.77$	39/33 = $\checkmark 1.19$	20/21 = $\checkmark 0.97$	8/5 = $\checkmark 1.76$

- Loglinear model: interactions with \*Nasal are non-significant, with mostly positive coefficients (combinations slightly overattested)
- Conclusion: cumulative rarity alone is not enough to cause disproportionate underattestation

(27) Claim: a grammatical effect

- Although nasals are somewhat low in type frequency in Lakhota, they are not subject to all that many phonological restrictions
  - Can occur freely in roots, prefixes, and suffixes
  - Low type freq. due to small inventory of nasal place contrasts, rather than dislike of nasals
- The insight that this leads to: degree of underattestation of a combination follows from strength of **grammatical** constraints against the elements involved, not low frequency per se

(28) Summarizing this result

- Cumulative effects: dispreferred elements cooccur even less often than expected, based on degree of dispreference for either one independently
- Leads to appearance of ‘complexity threshold’: marked structures may occur individually, but combinations are restricted
- Crucially, not as simple as saying that combinations of rare things are extra-rare
  - Nasals are relatively infrequent, but not grammatically restricted; no cumulative effects
- We need a grammatical analysis that can distinguish markedness (=strength of grammatical penalty) from frequency (=observed probability)

### 2.3 Capturing cumulative interactions with an additive constraint model

(29) The challenge

- Allow some combinations of marked structures to occur as often as expected based on independent probability, while other combinations receive an additional penalty
- Degree of cumulative effect should follow from grammatical status of subparts
  - Combinations of things which are already marginal become even worse

- Effect is lexically gradient—perhaps universally so?
- A root/morpheme structure effect: no alternations
- In this section, we generate a lexicon with these properties, using a grammar of weighted constraints (Harmonic Grammar: Legendre, Miyata, and Smolensky 1990; Pater 2010)

(30) Such interactions cannot be derived in OT

- CC clusters tolerated: DEP(ə) ≫ \*[CC]
- Fricatives tolerated: IDENT([±cont]) ≫ \*Fric

/kpā/ ‘fine’	DEP(ə)	*[CC]
☞ a. kpā		*
b. kəpā	*!	

/maza/ ‘metal’	IDENT([±cont])	*Fric
☞ a. maza		*
b. mata	*!	

- Both automatically tolerated simultaneously

/kpaza/ ‘dark’	DEP(ə)	IDENT([±cont])	*[CC]	*Fric
☞ a. kpaza			*	*
b. kəpaza	*!			*
c. kpata		*!	*	
d. kəpata	*(!)	*(!)		

- Presence of one violation can’t ‘strengthen’ severity of the other
- Put differently: \*[CC and \*Fricative violations can’t “gang up” to require a repair

(31) Conjoined constraints are not the answer

- Narrowly speaking, it would be possible to capture the observed cooccurrence restrictions with conjoined constraints

/kpaza/ ‘dark’	*[CC & *Fric	DEP(ə)	IDENT([±cont])	*[CC]	*Fric
a. kpaza	*!			*	*
☞ b. kəpaza		*			*
☞ c. kpata			*	*	
d. kəpata		*(!)	*(!)		

- However, this would fail to capture several key aspects of the pattern
  - Conjoined constraint is an independent parameter—no necessary relation between ranking of \*X&\*Y and subparts \*X, \*Y
  - Could produce categorical phonotactic restrictions as well as gradient ones
  - Could produce alternations in complex words
- Conjoined constraints are too powerful a mechanism for deriving cumulative effects
  - We need something that allows the penalty of two violations to depend on the penalty of the components

(32) Weighted constraint models: promising, but not an automatic solution

- Harmonic Grammar (Legendre, Miyata, and Smolensky 1990; Pater 2010)
  - Constraints are assigned numerical weights
  - For each candidate, constraint violations are multiplied by weights, and then summed
  - Promising: sum of multiple violations > individual violations

- Pater (2010): Markedness and Faith violations trade off, precluding many cumulative effects

/kpaza/ ‘dark’ Weight:	DEP(ə)	IDENT([± cont])	*[CC]	*Fric	Sum
☞ a. kpaza			-1	-1	-4
b. kəpaza	-1			-1	-5
c. kpata		-1	-1		-5
d. kəpata	-1	-1			-6

- Repairing multiple  $\mathcal{M}$  violations often requires an equivalent number of  $\mathcal{F}$  violations
- $w(\mathcal{F}) > w(\mathcal{M}) \rightarrow 2w(\mathcal{F}) > 2w(\mathcal{M})$

- If we want multiple markedness violations to gang up, we need to sidestep this trade-off between Markedness and Faithfulness

(33) Redefining the competition: the null parse

- Main task for producing a lexicon: determine well-formedness of strings
  - [blɪk] is well-formed, [bwɪk] is marginal, [bnɪk] is illegal
- Unfaithful mappings (converting ill-formed strings to well-formed ones) are needed elsewhere
  - Repair structures created by morpheme concatenation (\*[kɪk-d] → [kɪkt])
  - Loanword adaptation (Dnieper → [nɪpɪ], [dənɪpɪ])
  - Let’s set these aside for now, and focus on producing a lexicon that obeys static restrictions<sup>3</sup>
- Elimination of possible words: losing to the null parse (Prince and Smolensky 2004)
  - Null candidate represents no output (‘gap’)
  - Escapes all markedness violations, except a single violation of the constraint MPARSE
- Schematically:
  - Fricatives allowed: Weight(MParse) > Weight(\*Fricative)

/yã/	MPARSE	*[CC]	*FRIC	Total
Weight:	4	3	3	
☞ a. yã		-1		-3
b. null	-1			-4

- Clusters allowed: Weight(MParse) > Weight(\*[CC])

/gla/	MPARSE:4	*[CC:3]	*FRIC:3	Total
☞ a. gla		-1		-3
b. null	-1			-4

- Combinations not allowed: Weight(\*[CC]) + Weight(\*Fricative) > Weight(MParse)

/yãgla/	MPARSE:4	*[CC:3]	*FRIC:3	Total
a. yãgla		-1	-1	-6
☞ b. null	-1			-4

- Two issues
  - Need the effect to be gradient, not categorical
  - Need to ensure that only those structures which are independently marginal can lead to cumulative effects

<sup>3</sup>For an approach that allows cumulative effects with standard faithfulness constraints, see Albright, Magri, and Michaels (2008)

## (34) Gradient well-formedness

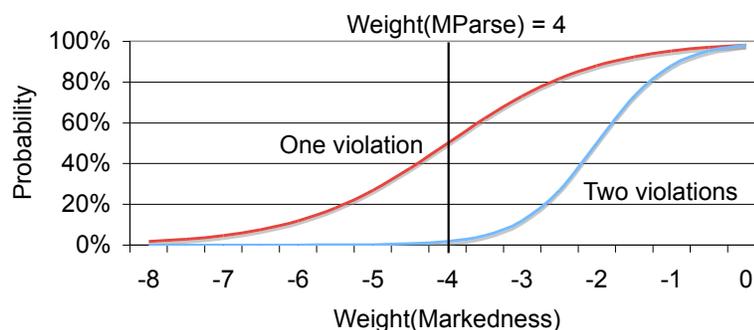
- The tableaux above simply assume that the candidate with the smallest penalty wins
- Following Maximum Entropy approaches (Goldwater and Johnson 2003; Jäger 2007):

$$\text{Prob}(\text{output}) = \frac{e^{\text{penalty}(\text{output})}}{\sum_{\text{candidates}} e^{\text{penalty}(\text{candidate})}}$$

- Penalty = weighted sum of violations
- For the schematic examples above:
  - Prob( $\gamma\bar{a}$ ), Prob( $g\bar{l}a$ )  $\approx$  73%
  - Prob( $\gamma\bar{a}g\bar{l}a$ )  $\approx$  12%

## (35) The poor get poorer

- Under the scheme in (34), the farther the weight of a markedness constraint is below MParse, the more likely the structure is to surface
- However, this condition also makes it relatively unlikely that the markedness constraint can gang up to overcome MParse (e.g.,  $2 \times \text{Weight}(\text{Markedness}) > \text{Weight}(\text{MParse})$ )
- Gang effects occur in a relatively small band around the weight of MParse



- Discrepancy between probability of one vs. two violations is most noticeable when Weight(Markedness) is close to MParse
- Probability of single violation is also beginning to decline at this point
- Captures observation that cumulative effects are seen only for structures that are already penalized individually by the grammar

## (36) Local summary

- Grammar of weighted constraints penalizes outputs with multiple violations more severely than outputs with single violations
- Weight of threshold constraint (MPARSE) establishes (gradient) cut-off
  - Grammar probabilistically eliminates inputs, based on severity of markedness violations
  - Eliminates = selects the null parse instead (i.e., produces no overt output)
  - The fact that the null parse violates just one constraint (MParse) allows multiple markedness violations to gang up and produce cumulative effects
- Strength of cumulative effect depends directly on strength of simpler effects
  - Summed violations of simpler constraints
  - Cumulative effect not learned separately; follows from weights of individual constraints
  - Precludes large disparities between well-formedness of single vs. multiple violations
  - Predicts that cumulative effects should be primarily or exclusively gradient

## 2.4 Using this mechanism to produce the Lakhota pattern

### (37) Deriving cumulative interactions with MParse

- The loglinear model at the end of section 2.1 is formally equivalent to a MaxEnt grammar, using the relevant factors as constraints
- In that section, we tested for cumulative effects by including factors for interactions
  - \*CC...CC, \*CC...Fric/Fric...CC, etc.
- In this section, we derive such effects with a simpler model, employing MPARSE

### (38) Input to the model

- 257 schematic root types described above, with their type frequencies in the Lakhota lexicon
- Constraints:
  - Markedness constraints on simple structures (fricatives, aspirates, ejectives, nasals, various cluster types, etc.)
  - MPARSE
- Each attested root type competes with a “null” candidate

/TLVSV/	Freq	MPARSE	*[CC	*FRIC	etc...
a. TLVSV	10		-1	-1	
b. <i>null</i>		-1			

- Initial bias:  $\text{weight}(\text{MPARSE}) > \text{weight}(\mathcal{M})$ 
  - Model is biased not to produce structures unless there is positive evidence for them<sup>4</sup>
  - $\text{Weight}(\mathcal{M}) = 10$
  - $\text{Weight}(\text{MPARSE}) = 5$
- Learning: MaxEnt Grammar Tool (Hayes, Wilson, and George 2009)

### (39) The resulting grammar

Constraint	Weight	
MPARSE	Penalizes null output	16.34
*TN	*Stop + nasal	8.86
*SN	*Fricative + nasal	8.85
*Ejective		8.62
*SR	*Fricative + liquid/glide	8.49
*TT	*Stop + stop	8.44
*ST	*Fricative + stop	8.24
*Asp	*Aspirated [–strid] stop	7.63
*TR	*Stop + liquid/glide	7.13
*SV	*Prevoalcalic fricative (McAllister 2009)	6.95
*Glide		6.06
*Lateral		5.98
*Nasal		5.25
*CC		0.00
*Stop		0.00

<sup>4</sup>Technically, this is implemented by assigning mean “target” values for weights ( $\mu$ ), as shown above, plus standard distributions that determine how strictly the model is constrained to find weights around those values ( $\sigma^2 = .1$ ).

- Weight of MPARSE violation is substantially above weights of other violations, independently
- However, rarer structures have weights  $> .5 \times \text{weight}(\text{MPARSE})$
- This puts multiple violations within ‘striking distance’ to overcome MPARSE

(40) Predictions of the grammar: probability of output (representative selection)

Simple		With self		Other combinations			
NV	100%	NVNV	100%	NVT <sup>h</sup> V	97%	NVSV	98%
SV	100%	SVSV	92%	SVT <sup>h</sup> V	85%	SVTTV	72%
T <sup>h</sup> V	100%	T <sup>h</sup> VT <sup>h</sup> V	75%	T <sup>h</sup> VSV	85%	T <sup>h</sup> VTTV	43%
TTV	100%	TTVTTV	37%	TTVSV	72%	TTVT <sup>h</sup> V	43%

- All simple structures assigned 100% probability
- Combinations with nasals not significantly penalized
- Other combinations penalized to varying extents (clusters  $>$  aspirates, fricatives  $>$  nasals)
  - Exact probability depends on parameters of the model; have not attempted here to match lexical probabilities precisely

(41) Summary of this section

- Schematic illustration of how a grammar of weighted constraints, including MPARSE, can yield cumulative effects
- Strength of the effect depends on weight of constraints on simple structures
- Qualitative match to observed effect: combinations of dispreferred structures are even more strongly underattested

### 3 English cluster combinations

#### 3.1 Cumulative effects in the English lexicon

English also shows (gradient) cumulative effects

(42) A widely discussed effect: clusters + OCP

- OCP violations are underattested, but legal in English (Berkley 2000)
  - *pipe, beep, bib, mime, kick, cake, gag, gang...*
  - *lull, loll, rare, roar*
- Non-coronal #sC clusters are also somewhat underattested, but fine
  - *spy, spike, sky, skate*
- Combinations of the two are rare or missing
  - \*spVp, \*skVk, \*slVl (also: \*plVl) (Browne 1981; Davis 1984; Frisch 1996; Coetzee 2008)
- Frisch (1996): such combinations are rarer than expected, given independent frequency of clusters and OCP violations

(43) Another (previously unnoticed?) example: CR...sC

- English has words that begin with obstruent+liquid clusters
  - pr, pl, br, bl, fr, fl, etc.

- English has words that end with *s*+stop clusters
  - *sp, st, sk*
- Surprisingly few words with *Cr...sC* combinations
  - *clasp, trust, grist*
  - Many combinations completely lacking, esp. with *Cl-*: *\*pIVsk, \*pIVst, \*bIVsk, \*gIVsp, \*gIVst*

## (44) The general claim

- Certain combinations, such as *CR...sC*, are unexpectedly rare in English, relative to frequency of subparts
- However, not sufficient to simply point out that there are no words like *\*[plɪsk]*, *\*[drʌsk]*, etc.
- As with Lakhota, we must show that there are fewer than expected
- Compare: no words like *\*[sfælk]*, *\*[sfɪlt]*, but this is unsurprising, since *#sf* words are rare to begin with

## (45) Testing this effect with a loglinear model

- Took all attested onsets and codas in monosyllabic lemmas listed in CELEX (Baayen, Piepenbrock, and van Rijn 1993)
  - Final *r*-clusters not present in CELEX transcription; recovered from orthography
- For each logically possible combination (*n*=7081), took type count of lemmas
  - Some combinations quite frequent: 28 *fVl*, 25 *rVt*, 23 *bVt*, etc.)
  - Most (*n*=5565) are unattested: *zVrv, nVsp, grVsk*
  - Some gaps are principled (*\*skVk, \*kIVl*, etc.), but many (most?) are arguably accidental
- As above, goal of model is to predict relative likelihood of different combinations

## (46) The baseline model: constraints on individual structures

- Coded ‘coarsely’ in order to avoid overfitting
  - Heuristic: categories that define categorical restrictions in English cluster types
  - *P, B* = stops, *F* = fricative, *N* = nasal
- Segment identity: positional (onset, coda)
  - Stop, affricate, fricative, voiced fricative, nasal, *l, r, s*
- Syllable structure:
  - Onset, Coda, Complex Onset, Complex Coda
- Cluster types
  - Onset: *Pr, Br, Fr, Pl, Bl, Fl, sp, st, sk, sN*
  - Coda: *lP, lB, lF, lN, rP, rB, rF, rN, sp, st, sk, NP, NB, NF, PP, PS*
  - Coda obstruent+obstruent, voiced obstruent+obstruent
- Baseline model: predicts some differences in rates of attestation, based on frequencies of parts

## (47) A relevant phonotactic restriction: OCP

- Many cluster-cluster combinations incur OCP violations
  - *smVmp, spVlp, prVsp*, etc.
  - As discussed, these are well known to affect rate of attestation

- Added factors for simple OCP violations
  - Place: OCP(lab), OCP(dors), OCP(cor)
  - Manner: lVl, rVr, sVs
- Result: small but significant improvement ( $p(> |\chi|) < .0001$ )

## (48) Cumulative effects: \*CR...CC

- Added factors for combinations of clusters
  - ClVsC, CrVsC, ClVNC, CrVNC
  - Question: are words like *blVsk*, *skVlt* significantly underattested?
- Result: significant improvement ( $p(> |\chi|) < .01$ )
- However, effect is seen only for some combinations
  - ClVsC significantly underattested ( $p(> |\chi|) < .01$ ), but CrVsC not ( $p(> |\chi|) = .9$ )
  - Combinations with nasal clusters are *overattested* (ClVNC:  $p(> |\chi|) < .005$ ; CrVNC n.s.)

## (49) Summary of this section

- Gradient cumulative effects also seen in the English lexicon
- As with Lakhota, some combinations strongly underattested, while others occur as often (or even more often) than expected
  - #Cl clusters, but not #Cr clusters
  - sC# clusters, but not NC# clusters
- General line of attack:
  - Derive penalty for combinations from penalty on simple structures
  - For this to work: grammar of English must prefer #Cr, NC# over #Cl, sC#
- On-going project: does this preference fall out from the lexical statistics of English, or does it reflect a phonological preference?

### 3.2 Cumulative effects in acceptability judgments

## (50) Testing for speaker knowledge of cumulative effects

- Strategy: make up nonce words with one or two clusters
 

Onset CC	brVC, spVC, dwVC, ...
Coda CC	CVmp, CVnt, CVsp, ...
Both	brVmp, blVnt, dwVsp, ...
- Ratings of brVC, brVCC, etc. allow us to estimate the weight of \*br
- Ratings of CVnd<sub>3</sub>, CCVnd<sub>3</sub>, etc. allow us to estimate the weight of \*nd<sub>3</sub>
- Question: do these values suffice to predict the rating of brVnd<sub>3</sub>?
  - Or, is the rating of brVnd<sub>3</sub> even lower than expected based on its parts?

## (51) A nonce-word acceptability experiment

44	Onset CC only	pl, kl, bl, gl, pr, kr, br, gr, kw, θw	bɛn, blɔs, klædʒ, dwɛp, ...
26	Coda CC only	mp, nt, nd <sub>3</sub> , sp, st, sk, lk	dɛmp, lænt, ɛndʒ, kɛst, ...
41	Onset + Coda CC	Combinations (non-identical place)	bɹæsk, blɛnt, klɛsp, dwɪmp, ...

- Also 78 fillers (no clusters, non-English clusters)

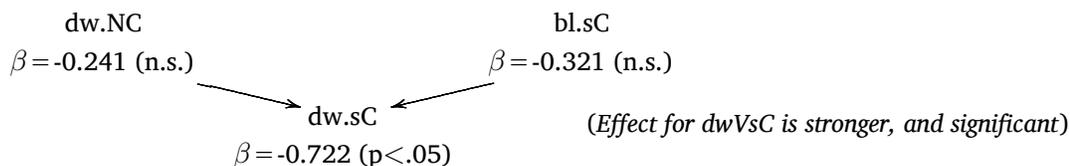


(55) Which combinations are penalized?

- Claim above: combinations of independently bad structures are even worse than expected
- Comparison

	Coda	✓NC	? sC
Onset	✓bl	blVNC	blVsC
	? dw	dwVNC	dwVsC

- Coding above is slightly too coarse to test this, since classes “Cr”, “Cl”, “Cw” are not homogenous groups (e.g., kw > dw > θw)
- Refitted model, with just factors penalizing specific cluster combinations:



## 4 Summary and discussion

(56) Cumulative interactions of markedness constraints

- Doubly marked structures less good than expected, given independent acceptability of subparts
- Seen in lexical counts, acceptability ratings
- Not discussed here: also seen in child simplifications (Levelt, Schiller, and Levelt 2000; Albright, Magri, and Michaels 2008)
- An underdocumented, but perhaps quite prevalent effect

(57) Analytical challenges

- Explain why markedness violations can gang up to produce static phonotactic effects, but evidently do not lead to repairs or alternations
- Explain why cumulative effects are seen for some combinations, but not others

(58) Pieces of the account

- Grammar of weighted constraints
  - Multiple violations may sum across the word
  - Creates potential to make multiple violations worse than single violations
- Competition with null candidate derives lexical underattestation
  - Weight of MPARSE constraint establishes ‘complexity threshold’
- An intrinsically gradient effect
  - Nature of competition in MaxEnt models means that doubly marked structures will be penalized only if singly marked structures are already somewhat degraded
  - Strength of effect depends on status of independent subparts

- (59) An immediate question: more dramatic effects for triply-marked structures (and beyond)?
- A perennial worry about additive models: elaborate counting effects
    - “Morphemes may have three but not four fricatives”
    - “Morphemes may have at most two instances of: fricatives, aspirates, or clusters”
  - The proposed model does indeed predict such effects—e.g., Lakhota:
    - $4 \times \text{Weight}(*\text{Nasal}) > \text{Weight}(\text{MPARSE}) > 3 \times \text{Weight}(*\text{Nasal})$
    - $\text{Weight}(*\text{Nasal}) + \text{Weight}(*\text{Lateral}) + \text{Weight}(*\text{Aspirate}) > \text{Weight}(\text{MPARSE})$
  - It’s conceivable that such effects really do occur
    - Hard to evaluate based on lexical counts, because expected frequencies of such words are already very low
    - Intuitively, hypothetical words can become quite unacceptable when they involve multiple independently OK structures: English [səˈflʊk], [ˈtækɹəp]
- (60) The relation between static phonotactics and alternations
- The mechanism proposed here cannot derive alternations
    - Pater (2009): once faithfulness is involved, violations ‘trade off’ in a way that precludes different repairs depending on number of markedness violations
  - This seems good: evidently no alternations triggered by cumulative complexity thresholds
    - ...and they probably would have been noticed, since alternations have been examined more comprehensively than static phonotactics<sup>5</sup>
  - But why don’t we simply get paradigm gaps when affixed words reach the threshold?
  - One possibility: different levels of evaluation
    - Root-level evaluation of ‘Morpheme Structure Constraints’ vs. stem/word-level evaluation of morphologically composed forms
  - Another possibility: threshold increases with morphological complexity
    - Null output for bimorphemic word = two ‘MPARSE’ violations
- (61) Future work
- Further experimental work: to what extent do speakers encode such effects?
    - Lexicon is gappy, hard to test predictions about combinations already predicted to be rare
    - Results above indicate that speakers do dislike words like *drusk* more than expected based on subparts
    - Need broader confirmation, with a wider variety of combinations
  - What kinds of violations can interact?
    - Examples tested here involve ‘similar’ structures (consonants; onset, coda clusters)
    - Model is quite general, and predicts broader range of effects

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<sup>5</sup>Though for a possible example, see Green (2010)

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